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**MATHEMATICS (SYLLABUS D)**

**4024/21**

Paper 2

**May/June 2018**

MARK SCHEME

Maximum Mark: 100

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**Abbreviations**

|      |                            |
|------|----------------------------|
| cao  | correct answer only        |
| dep  | dependent                  |
| FT   | follow through after error |
| isw  | ignore subsequent working  |
| oe   | or equivalent              |
| SC   | Special Case               |
| nfww | not from wrong working     |
| soi  | seen or implied            |

| Question  | Answer                        | Marks | Partial Marks   |
|-----------|-------------------------------|-------|---|
| 1(a)      | $(P \cup Q)'$ or $P' \cap Q'$ | 1     |   |
| 1(b)(i)   |                               | 2     | <b>B1</b> for 8 or more correct   |
| 1(b)(ii)  | 4                             | 1     | FT <i>their</i> Venn diagram provided no repeated elements  |
| 1(b)(iii) | 1                             | 1     | FT <i>their</i> Venn diagram provided no repeated elements  |
| 1(b)(iv)  | $A' \cap B \cap C$            | 1     |   |
| 1(c)(i)   | $2^2 \times 3^3 \times 5$     | 2     | <b>M1</b> for at least two correct stages in factor tree or ladder method   |
| 1(c)(ii)  | $2 \times 3^2 \times 5$       | 2     | <b>B1</b> for 90 seen or $2^2 \times 3^4 \times 5^2$  |
| 2(a)      | 109.95 or 109.96              | 3     | <b>B2</b> for 2109.9(..) or 2110<br>or <b>M2</b> for $2000 \left(1 + \frac{1.8}{100}\right)^3 - 2000$ oe<br>or <b>M1</b> for $2000 \left(1 + \frac{1.8}{100}\right)^3$ oe           |
| 2(b)      | 600                           | 3     | <b>M1</b> for $54 \times 12$ (=648)<br>or $\frac{54}{1.08}$ (=50) oe<br><b>M1</b> for $\left(\frac{100+8}{100}\right)x = \text{their} 648$ oe soi<br>or <i>their</i> $50 \times 12$ |
| 3(a)      | 9.5 oe                        | 2     | <b>M1</b> for $4p - 2p = 7 + 12$ or better  |

| Question  | Answer   | Marks     | Partial Marks  |
|-----------|--|-----------|--|
| 3(b)      | Correct method to eliminate one variable                                     | <b>M1</b> |  |
|           | $x = 1, y = -3$  | <b>A2</b> | <b>A1</b> for $x = 1$ or $y = -3$<br>After <b>A0</b> , <b>SC1</b> for two correct values with no working or two values that satisfy one of the original equations  |
| 3(c)      | $\frac{m}{2m-1}$ final answer nfw  | <b>3</b>  | <b>B1</b> for $m(m+3)$<br><b>B1</b> for $(2m-1)(m+3)$  |
| 3(d)      | 62.5 oe  | <b>3</b>  | <b>M2</b> for $b = \frac{4}{8} \times (5)^3$ oe soi<br>or <b>B1</b> for $\frac{4}{8}$ oe or $\left(\frac{5}{2}\right)^3$ oe soi or $b = ka^3$  |
| 4(a)      | $\frac{1}{6}$ cao  | <b>1</b>  |  |
| 4(b)      | $\frac{1}{660}$ oe   | <b>2</b>  | <b>M1</b> for $\frac{1}{12} \times \frac{1}{11} \times \frac{2}{10}$ oe<br>or <b>SC1</b> for $\frac{1}{12} \times \frac{1}{12} \times \frac{2}{12}$ or answer $\frac{1}{864}$<br>or $\frac{1}{12}, \frac{1}{11}, \frac{2}{10}$ |
| 4(c)(i)   | $\frac{8}{12}, \frac{8}{11}, \frac{4}{11}, \frac{7}{11}$ oe correctly placed | <b>2</b>  | <b>B1</b> for two correct  |
| 4(c)(ii)  | $\frac{1}{11}$ oe  | <b>1</b>  |  |
| 4(c)(iii) | $\frac{16}{33}$ oe   | <b>2</b>  | <b>M1</b> for $\frac{4}{12} \times \frac{8}{11}$ or $\frac{8}{12} \times \frac{4}{11}$ oe  |
| 5(a)(i)   | $6n - 5$ oe  | <b>2</b>  | <b>M1</b> for $6n + k$ oe with $k \neq 0$  |
| 5(a)(ii)  | 256 is not exactly divisible by 6 or 247 in sequence and next one is 253 oe  | <b>1</b>  |  |
| 5(b)(i)   | $p^2 - 3$ oe   | <b>1</b>  |  |
| 5(b)(ii)  | $p^2 + 2p + 4$ oe  | <b>1</b>  |  |
| 5(c)(i)   | Correct drawing  | <b>1</b>  |  |
| 5(c)(ii)  | 28, 40   | <b>2</b>  | <b>B1</b> for one correct  |
| 5(c)(iii) | $t^2 + 3t$ oe  | <b>2</b>  | <b>B1</b> for $t^2 + \dots$  |
| 6(a)(i)   | Correct construction with arcs   | <b>2</b>  | <b>B1</b> for correct triangle with arcs missing or arc 6 cm from $A$ or arc 9 cm from $B$   |

| Question  | Answer   | Marks     | Partial Marks   |
|-----------|--|-----------|---|
| 6(a)(ii)  | $77^\circ$ to $81^\circ$   | 1         | FT <i>their</i> angle $BAC$   |
| 6(b)      | 79875 cao  | 2         | <b>B1</b> for 225 and 355 seen  |
| 6(c)(i)   | $66^\circ$ alternate [angles]  | 2         | <b>B1</b> for 66  |
| 6(c)(ii)  | $79^\circ$   | 1         | FT 145 – <i>their</i> 66  |
| 6(c)(iii) | $RQT$<br>$RTQ$   | <b>B1</b> |   |
|           | $QT$ is common oe  | <b>B1</b> |   |
|           | AAS oe   | <b>B1</b> | Dep on previous B1  |
| 7(a)      | $15 + [2 \times] 3x + [2 \times] \left(\frac{15}{x} \times 3\right)$ | <b>M1</b> |   |
|           | Leading to $\left(15 + 6x + \frac{90}{x}\right)$ without error       | <b>A1</b> |   |
| 7(b)      | 5.70 or 2.63<br>and $6x^2 - 50x + 90 [= 0]$ seen                     | 4         | <b>B1</b> for $6x^2 - 50x + 90 [= 0]$ oe<br>AND<br><b>B2FT</b> for $\frac{-(-50) \pm \sqrt{(-50)^2 - 4 \times 6 \times 90}}{2 \times 6}$<br>or <b>B1FT</b> for $\sqrt{(-50)^2 - 4 \times 6 \times 90}$<br>or $\frac{-(-50) \pm \sqrt{r}}{2 \times 6}$<br>After 0, <b>SC2</b> for 5.70 or 2.63 |
| 7(c)(i)   | 74.25  | 1         |   |
| 7(c)(ii)  | Correct smooth curve   | 2         | <b>B1FT</b> for at least 5 points correctly plotted   |
| 7(c)(iii) | 6.5 to 6.6<br>2.3 to 2.4   | 2         | FT <i>their</i> graph<br><b>B1FT</b> for either correct   |
| 8(a)      | $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$                      | 2         | <b>B1</b> for a correct row or column   |
| 8(b)      | Triangle with vertices at $(2, -3)$ $(4, -3)$<br>$(2, -4)$           | 1         |   |
| 8(c)      | Reflection in $y = x$  | 2         | <b>B1</b> for reflection or $y = x$   |
| 8(d)      | Rectangle with vertices at<br>$(-1, 5)$ $(-1, 6)$ $(2, 6)$ $(2, 5)$  | 2         | <b>B1</b> for $R$ translated by $\begin{pmatrix} -2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$   |

| Question  | Answer                        | Marks     | Partial Marks  |
|-----------|-------------------------------|-----------|--|
| 9(a)      | 9.025 to 9.03                 | 4         | <b>M3</b> for $\frac{70}{360} \times \pi \times 8^2 - \frac{1}{2} \times 8^2 \times \sin 70$<br>or<br><b>M1</b> for $\frac{70}{360} \times \pi \times 8^2$<br><b>M1</b> for $\frac{1}{2} \times 8^2 \times \sin 70$  |
| 9(b)(i)   | 8 – 8cos 35 oe                | <b>M2</b> | <b>M1</b> for 8cos 35 (= 6.55..)   |
|           | 1.45 or 1.446 to 1.447 so yes | <b>A1</b> |  |
| 9(b)(ii)  | 192                           | 2         | <b>B1</b> for two of 4, 16 and 3 soi<br>or <b>M1</b> for $\frac{48 \times 4x \times 24}{16 \times x \times 1.5}$ oe  |
| 10(a)     | 11 13                         | 2         | <b>M1</b> for $\frac{12}{15}[\times 60]$ oe  |
| 10(b)     | 13.7 or 13.70...              | 4         | <b>B1</b> for 146°<br>AND<br><b>M2</b> for $\sqrt{12^2 + 2^2 - 2 \times 12 \times 2 \times \cos 146}$<br>or <b>M1</b> for $12^2 + 2^2 - 2 \times 12 \times 2 \times \cos 146$<br><br><i>Alternative</i><br><b>B1</b> for 9.95 or 9.948 to 9.949 or 6.71[0...]<br>AND<br><b>M2</b> for $\sqrt{\text{their } 6.71^2 + (\text{their } 9.94 + 2)^2}$<br>or <b>M1</b> for $\text{their } 6.71^2 + (\text{their } 9.94 + 2)^2$ |
| 10(c)     | 3.0 or 3.00 to 3.01           | 2         | <b>M1</b> for $\tan .. = \frac{\text{figs } 105}{\text{figs } 2}$ oe   |
| 11(a)     | Correct region indicated      | 3         | <b>B1</b> for ruled line $x = 1$<br><b>B1</b> for ruled line $x + y = 5$   |
| 11(b)(i)  | 6.32...                       | 2         | <b>M1</b> for $\sqrt{(5 - (-1))^2 + (5 - 3)^2}$  |
| 11(b)(ii) | $y = -3x + 10$ oe             | 4         | <b>B3</b> for (2, 4) <b>and</b> $y = -3x + c$<br><br>OR<br><b>B2</b> for $y = -3x + c$<br><br>OR<br><b>B1</b> for (2, 4) or $\frac{5-3}{5-(-1)}$ oe<br>and <b>M1</b> for $-\frac{1}{\text{their } \frac{1}{3}}$  |