## MARK SCHEME for the October/November 2014 series

## 4040 STATISTICS

4040/13
Paper 1, maximum raw mark 100

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18 is the mode M1
The value which occurs most frequently. A1
9 is the median M1
Obtained by arranging the values in ascending or descending order and
selecting the 'middle' one. A1
11 is the (Arithmetic) mean M1
Obtained by summing the numbers and then dividing by 13 A1

2 (i) X is discrete $\mathrm{B} 1^{*}$
Because it only takes integer values (or equivalent comment) B1dep
(ii) 0 and 4 (B1 for each) B2
(iii)

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 0 | 5 | 15 | 10 | 0 | 7 | 6 | 7 |

(-1 each independent error)

3 (a) Similar in that both would sample proportionately from the different age groups. B1
In stratified sampling interviewers would be given a list of specific people to interview, in quota sampling the interviewer selects the individuals.
(b) (i) Because the last page of a chapter is less likely than all other others to be filled with words, B1
the sample is likely to be biased. B1
(ii) A systematic sample is a form of random sampling B1
and so unless there is some pattern in the pages which matches the sampling interval the sample will be unbiased.
(ii) All points plotted correctly both horizontally and vertically
(iii) (a) Correct reading from graph of a point between cum. freqs. 12 and $13 \quad$ B1 $\sqrt{\text { }}$
(b) Clear attempt to use appropriate point on the graph and any valid method to find the required percentage.

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5 (i) Advantage: it shows actual amounts of wood. ..... B1
Disadvantage: it only shows information about individual sizes. ..... B1
(ii) The total amount of wood of all sizes produced. ..... B1
(iii) Pie chart ..... B1
Sectional (component) bar chart ..... B1
(iv) Change chart ..... B1
6 (i) Attempt to sum the values in the diagram and subtract the total from 70. ..... M1
5 ..... A1
(ii) None of the people in the sample speak all three languages. ..... B1
(iii) (a) No, because this person will still only speak two languages. ..... B1
(b) Yes, because the person now speaks all three languages. ..... B1
(c) No, as this person only speaks one of the three languages. ..... B1

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7 (a) Sight of $3 / 7$ used B1
EITHER 1 - sum of two two-factor products M1
$1-[(4 / 7 \times 1 / 5)+(3 / 7 \times 1 / 9)] \quad$ A1
88/105 A1
OR Sight of $4 / 5$ and $8 / 9$ used M1
$(4 / 7 \times 4 / 5)+(3 / 7 \times 8 / 9) \quad$ A1
88/105 A1
(b) (i) EITHER $3 / 7 \times 2 / 6 \times 1 / 5$ OR $1 / 7 \times 1 / 6 \times 1 / 5 \times 3$ ! M1
$1 / 35$ A1
(ii) Any appreciation of the fact that it is irrelevant which two are the brother and sister.

B1
EITHER $1 / 7 \times 1 / 6(\times 1) \times 3$ ! OR $5 / 7 \times 1 / 6 \times 1 / 5 \times 3$ ! M1
1/7
(c) (i) Clear attempt at both two blue and two white
$(2 / 8 \times 3 / 8)+(6 / 8 \times 5 / 8) \quad$ A1
9/16 A1
(ii) Given first balls were the same colour, $P$ (both were blue) $=1 / 6$, $P($ both were white $)=5 / 6$

Attempt to add probabilities relating to whether first balls were blue or white
$(1 / 6)[(3 / 9 \times 5 / 7)+(6 / 9 \times 2 / 7)]+(5 / 6)[(2 / 9 \times 4 / 7)+(7 / 9 \times 3 / 7)]$
$86 / 189=0.455$

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| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Time ( $x$ ) <br> (minutes) | Frequency ( $f$ ) | Mid-pts $(m)$ | $y$ | $f y$ | $f^{2}$ |
| $0-$ under 30 | 6 | 15 | -12 | -72 | 864 |
| $30-$ under 35 | 11 | 32.5 | -5 | -55 | 275 |
| $35-$ under 40 | 4 | 37.5 | -3 | -12 | 36 |
| $40-$ under 50 | 40 | 45 | 0 | 0 | 0 |
| $50-$ under 60 | 26 | 55 | 4 | 104 | 416 |
| $60-$ under 70 | 14 | 65 | 8 | 112 | 896 |
| $70-$ under 100 | 4 | 85 | 16 | 64 | 1024 |
| TOTAL | 105 |  |  | 141 | 3511 |

(i) Mid-points correct
(ii) Values of $y$ found correctly
y values correct
(iii) fy values found correctlyM1
(iv) $\mathrm{fy}^{2}$ values found correctly M1
(v) Summations correct
(vi) Use of their values in a correct method for mean of $y$

Mean of $y=1.34$
(vii) Use of their values in a correct formula for variance or s.d. of $y$
s.d. of $y=5.62$
(viii) (a) (Their y mean $\times 2.5$ ) +45
48.4
(b) (Their y s.d. $\times 2.5$ ) only
(ix) The distribution is reasonably symmetrical with relatively few extreme values, (or similar comment),
and so the s.d. is preferable to the IQR.

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9 (i) $36 \quad 32$ in second and third cells ..... B1
Any appreciation of area being proportional to frequency ..... M1
2428 in first and last cells ..... A1
$21 \quad 18 \quad 22 \quad 19$ in remaining cells ..... A1
(ii) Correct classes, 15-17, 17-19 etc. ..... M1
Correct frequencies 24688028 ..... A1
Their results presented in a suitable table ..... B1
(iii) Four rectangles of equal width ..... M1
Vertical axis correctly annotated ..... M1
Rectangles of correct heights ..... A1
(iv) Use of 'diagonal line' on histogram or equivalent numerical method seen ..... M1
19.35 cm ..... A1 ${ }^{\wedge}$
(v) Proportions of first and last classes found correctly ..... M1
Total cakes which can be sold found correctly ..... M1
Percentage expressed correctly ..... M1
84\% ..... A1
10 (i) $(3 \times 7)$ or $(3 \times 7000) / 1000$ or equivalent seen $\mathbf{A G}$ ..... B1
(ii) Total deaths $25+21+47+83(=176)$ ..... M1
Total population $4500+7000+6000+7000(=24500)$ ..... M1
CDR $=($ Total deaths $/$ Total population $) \times 1000$ ..... M1
$=7.18$ ..... A1
(iii) (Deaths/Population) $\times 1000$ seen for any age group (or can be implied by one correct result) ..... M1
$5.56 \quad 7.83 \quad 11.86$ all correct ..... A1
(iv) Rate $\times \mathrm{SP} \%$ seen for any age group (or can be implied by one correct result) ..... M1
Attempt to sum results for all age groups ..... M1
$5.56 \times 0.2+3 \times 0.35+7.83 \times 0.25+11.86 \times 0.2$ ..... A1
6.49 ..... A1
(v) Rate $\times \mathrm{SP} \%$ added for four groups ..... M1
7.90 ..... A1
(vi) Any valid comment relating to the towns having different age structures ..... B1
(vii) Because the SDR is lower ..... M1
Eastbury has the healthier environment. ..... A1

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11 (i) Correct plots (-1 each error) ..... B2
Correct labels ..... B1
(ii) $(37.5,104.5)$ ( B 1 each coordinate) ..... B2 ..... B1
(iii) Correct SA plots (B1 for each) ..... B2
Line of best fit through at least two averages ..... B1
(iv) A and $B$ results are both approximately linear. ..... B1
$C$ results are completely inconsistent. ..... B1
(v) Correct plot ..... B1
(vi) Experienced technician's result totally consistent with those of B, ..... B1
suggesting that B's observations are accurate. ..... B1
(vii) Line drawn through results of $B$ and the experienced technician ..... B1
(viii) 135 kg , with clear indication value found from use of the revised line ..... B1

