

# **Cambridge IGCSE**<sup>™</sup>

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

# 2730862341

#### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/52

Paper 5 Investigation (Core)

February/March 2022

1 hour 10 minutes

You must answer on the question paper.

No additional materials are needed.

#### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.

#### **INFORMATION**

- The total mark for this paper is 36.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 12 pages. Any blank pages are indicated.

# Answer **all** the questions.

#### INVESTIGATION

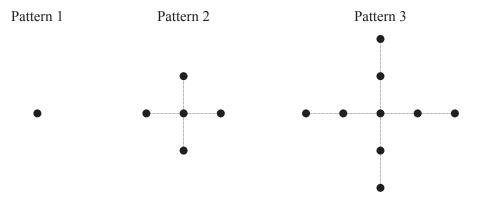
#### **DOT PATTERNS**

This investigation looks at patterns in sequences of dots, and of dots and crosses.

1	This is a sequence of dot pattern	S.
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	Pa	ttern 1	Pattern	2			Patte	rn 3		
(a)	Draw Pattern	• • • • • • • • • • • • • • • • • • •	•	•		•	•	•	•	
(b)	Complete the	e table.								[1]
		Pattern number, n	1	2	3	4	5	6		
		Number of dots	2	3	4					
(c)	How many d	ots are in Pattern 9?								[1]
										[1]
(d)	Write down a	an expression, in tern	ns of $n$ ,	for the	numbe	er of do	ots in P	attern <i>i</i>	$\eta$ .	
		•								
(e)	Find the num	nber of the pattern tha	at has 26	6 dots.						[1]
										[2]

2 This is another sequence of dot patterns.



(a) Complete the table.
You may use the grid below to help you.

Pattern number, <i>n</i>	1	2	3	4	5	6
Number of dots						21

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[3]

**(b)** Find an expression, in terms of n, for the number of dots in Pattern n.

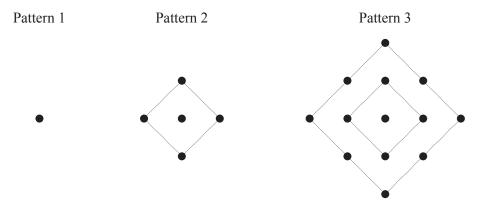
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(c) Work out the number of dots in Pattern 40.

.....[2]

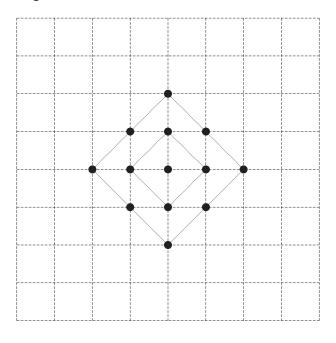
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3 (a) Oliver draws this sequence of patterns called *centred squares*.



(i) Pattern 3 is drawn on the grid.

Complete the diagram to show Pattern 4.



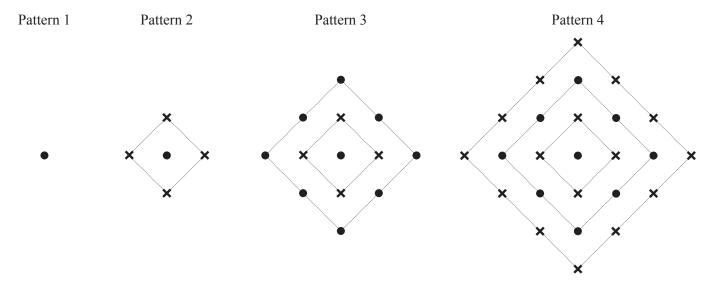
[1]

(ii) Complete the table.

Pattern number, <i>n</i>	1	2	3	4	5
Number of dots	1	5	13		

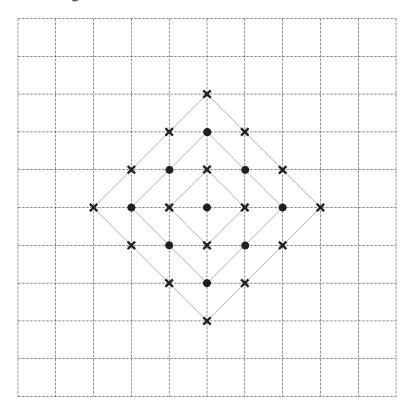
		[2]
(iii)	Work out the number of dots in Pattern 6.	
		[2]

**(b)** Oliver draws the patterns of centred squares using dots and crosses.



(i) Pattern 4 is drawn on the grid.

Complete the diagram to show Pattern 5.



[1]

## (ii) Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	1	0	1
2	1	4	5
3	9	4	13
4		16	
5			
6			

[3]

## (iii) Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	$1 = 1^2$	$0 = 0^2$	$1^2 + 0^2 = 1$
2	$1 = 1^2$	$4 = 2^2$	$2^2 + 1^2 = 5$
3	$9 = 3^2$	$4 = 2^2$	$3^2 + 2^2 = 13$
4		16 =	
5			
6			

[2]

(iv) Complete the formula for the total number of dots and crosses, T, in Pattern n.

 $T = \dots [2]$ 

4 Sophia draws the patterns of centred squares using dots and crosses in a different way.

Pattern 1 Pattern 2 Pattern 3 Pattern 4

# (a) Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	1	0	1
2	5	0	5
3	9	4	13
4	13		25
5			

**(b)** Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	1	$0 = 4 \times 0$	$1 + 4 \times 0 = 1$
2	5	$0 = 4 \times 0$	$5+4\times0=5$
3	9	$4 = 4 \times 1$	$9+4\times 1=13$
4	13	$12 = 4 \times (1+2)$	$13 + 4 \times (1 + 2) = 25$
5		$= 4 \times (1 + 2 + )$	+ =
6			

[3

(c)	(i)	In Sophia's patterns, Pattern <i>k</i> has 112 <b>crosses</b> .
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Find the value of k.

b	_	ГЗ:	1
n	_	 IJ	ı

(ii) Work out the total number of dots and crosses in Pattern k.

.....[2]

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